





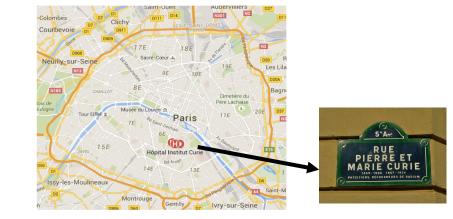
Computational methods for logical modelling applied to a model of the early steps of metastasis

Laurence Calzone 22 March 2018

Institut Curie







Research center

Hospital





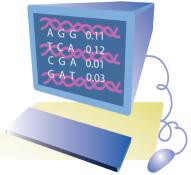
2100 members in the Hospital1100 members in the research center

Computational Systems Biology group

Objective of our group: based on existing knowledge and data, we would like to be able to explain **why** certain mutations of normal genome can lead to tumorigenesis, and **how** to reverse their effect



Formalizing biological knowledge Integrative analysis of omics data for cancer research

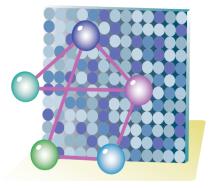


e.g. https://acsn.curie.fr/

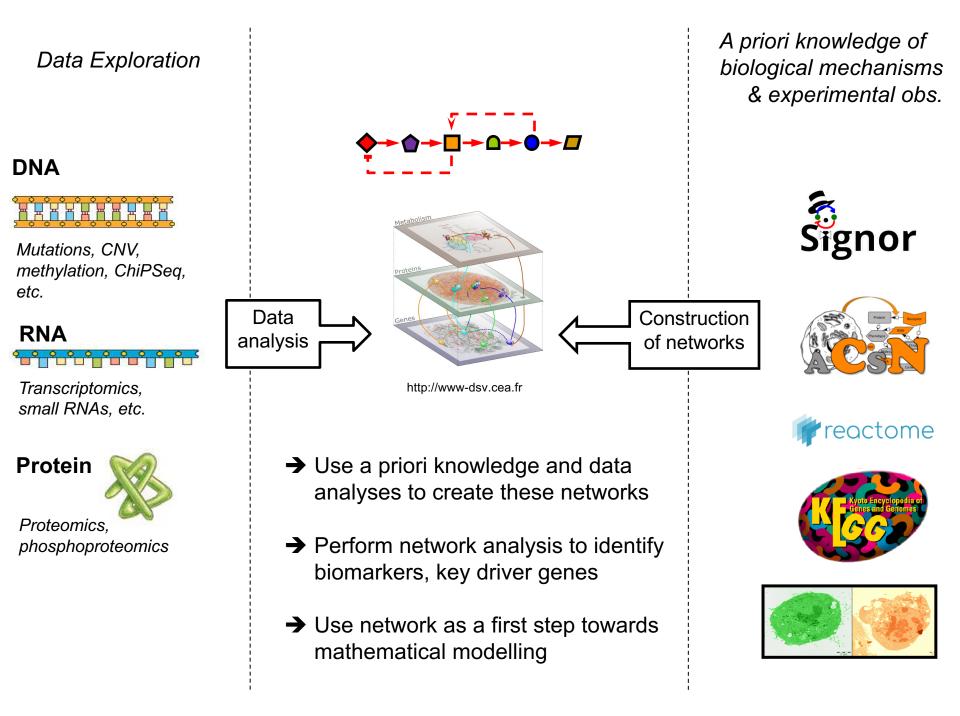


Mathematical modeling of cell fate decisions to understand cancer biology

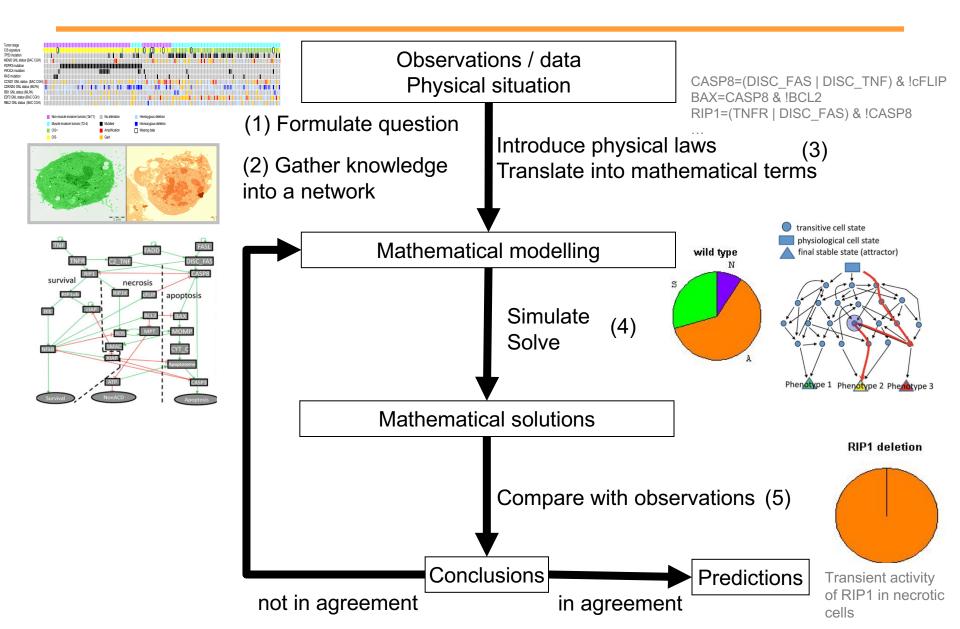
Computational methods for systems biology



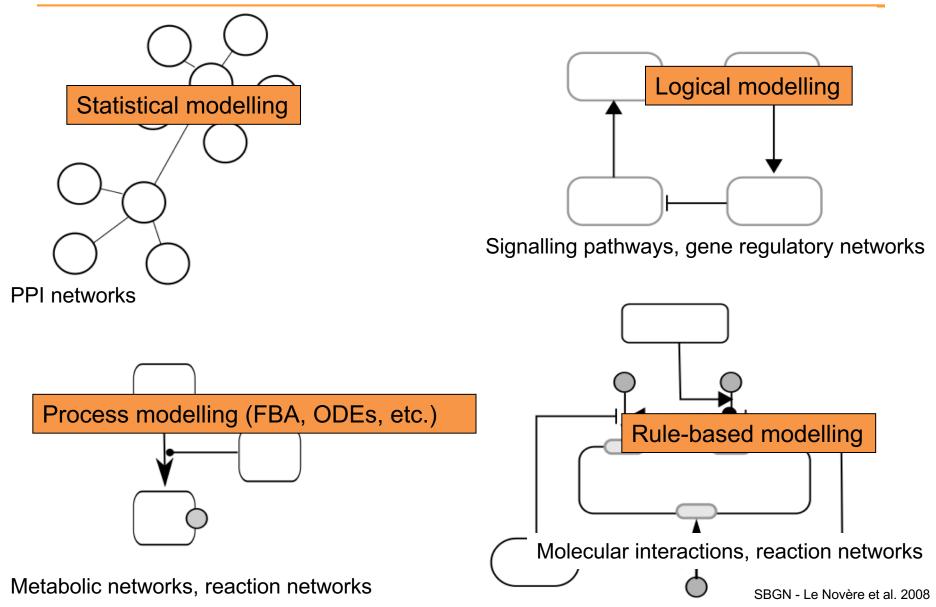
http://sysbio.curie.fr/



The modelling cycle



From a network to a model: different types of standard networks and their preferred formalism



Choosing the appropriate format for a mathematical model

Different formalisms:

- Logical
- ODEs (ordinary differential equations)
- PDEs (partial differential equations)
- Algebraic equations
- Cell automata
 - ...

Different types of simulations:

- Discrete approach
- Deterministic approach
- Stochastic approach
- ...

MODELLING

Quantitative and logic modelling of molecular and gene networks

Nicolas Le Novère

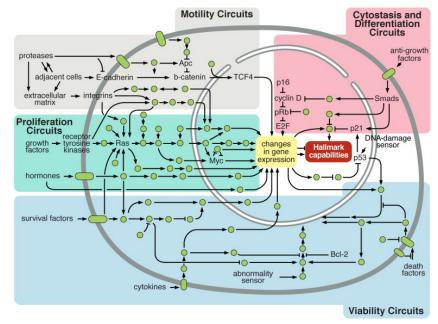
Nat Rev Genet. 2015 Mar;16(3):146-58.

Building a model in the context of cancer

- Summarize into a model (network) what is known about altered processes (including feedbacks)
- Understand the importance of alterations: mutations, copy number variations,...
- Identify the main players of a process
- Identify the possible intervention points: suggest single or combinations of drugs
- Anticipate effects of some drugs
- Explore effects of clonality
- Predict / explain mechanisms of resistance

« Cancer is a network disease »

Goh et al. PNAS, 2007



Hanahan and Weinberg, 2011

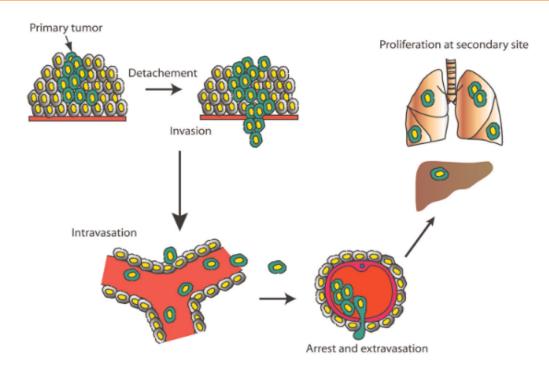
Application: How do the two signalling pathways, p53 and Notch, interact to trigger metastasis in colon cancer?
→ A logical model of early steps of metastasis

Methodology: How to automatize these analyses and extract knowledge and predictions from any logical model?

Application to cancer:

A logical model of the early steps of metastasis

Metastasis

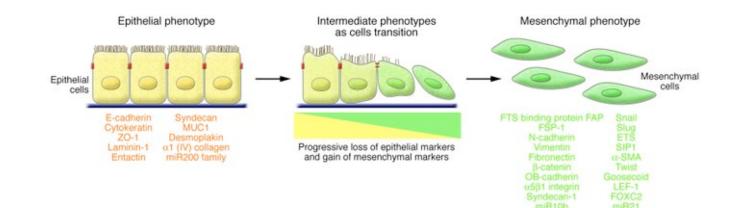


Cancer cell spreads from its primary site to a distant site It occurs through a series of steps:

- local invasion (of neighboring tissues),
- intravasation,
- transport (through the blood or the lymph system),
- extravasation (re-enter a distant tissue), and
- colonization.

Breast Cancer Research Vol 10 Suppl 1 Hunter et al.

EMT – the players



Kalluri and Weinberg (2009) J Clin Invest. 2009

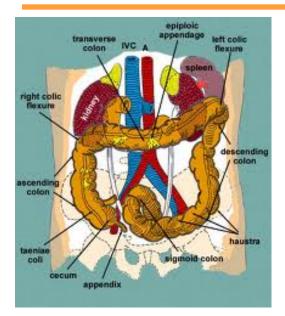
EMT (Epithelial to mesenchymal transition) is a biological process by which cells lose epithelial characteristics (e.g., cell-cell adhesion), gain invasive properties and acquire mesenchymal phenotype.

Apostolos Zaravinos, The Regulatory Role of MicroRNAs in EMT and Cancer. Journal of Oncology, Volume 2015, Article ID 865816

Colon cancer

Rectum (end of the colon)

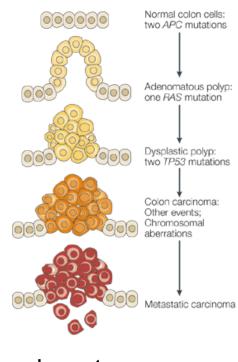
Affected area: Large intestine (colon),



Historically well studied: progressive accumulation of mutations, APC, RAS, p53

Experimental system:

mice with a possibility of conditional mutations in gut Nature Reviews I Cancer (villin-CreERT2 tamoxifen-dependent intestine-specific recombination)







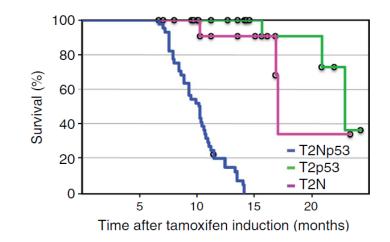


Mice model of colorectal cancer

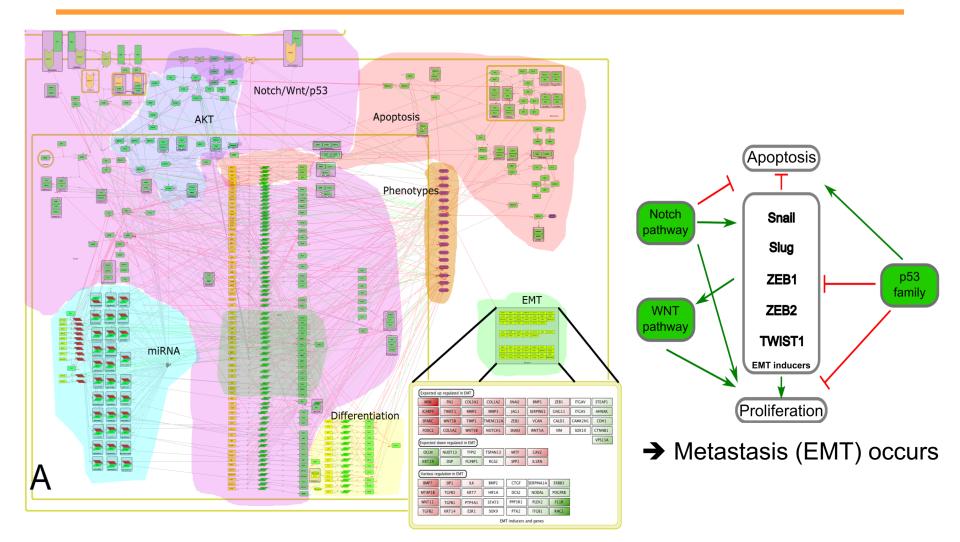
Experimental results:

Two signaling pathways, Notch and p53, are involved in triggering metastasis in mice

- Single mutations (NICD++ or p53--) do not induce metastases
- NICD++/p53-- mice developed adenocarcinoma 15 months post induction
- Compared to single mutant mice, double mutant mice show drastic decrease in survival

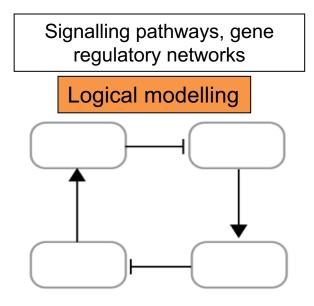


Network description and hypothesis



Notch – p53 map in Navicell www.navicell.curie.fr Can we formally confirm, with a mathematical model, the appearance of metastasis in mice carrying the double mutation: NICD +/+ p53 -/-?

Why to model with logical formalism?



In general:

- The question is qualitative
- The data are discrete (mutations, copy number, etc.)
- Expression data are not absolute values
- No information over time
- No details about the precise biochemical reactions

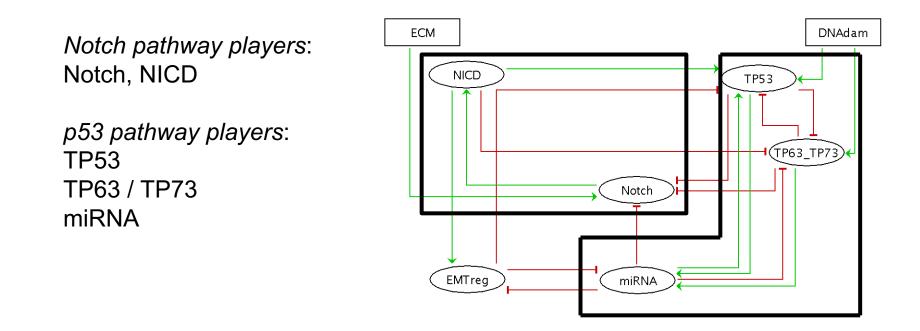
Here:

- The question is qualitative
- The data are phenotypes (or survival info)
- No information about time
- Only hand-waving hypotheses

A small network of the p53 and Notch pathway interactions

The hypothesis: the two pathways regulate the activity of the EMT regulators

- Notch pathway activates the EMT regulators
- p53 pathway inhibits the EMT regulators through miRNA



→ Translation into a logical model

The logical model

Boolean logic:

Connectors: AND (&), OR (|), NOT (!), XOR (/) Logic depends on incoming arrows

			ECM 1 DNAdam
ID	Val	Logical function	
NICD	1	• Notch	
Notch	1	• ECM & !miRNA & !TP63_TP73 & !TP53	
TP53	1	• (DNAdam NICD miRNA) & !EMTreg & !TP63_TP73	0 (TP63_TP73)
TP63_TP73	1	• DNAdam & !miRNA & !NICD & !TP53	
miRNA	1	• (TP53 TP63_TP73) & !EMTreg	
EMTreg	1	• NICD & !miRNA	EMTreg miRNA
DNAdam		no function	
ECM		no function	

Construction and first analyses of the model using



- Identifications of attractors* (solutions of system)
- Functionality of circuits

* *Attractors* are subgraphs of the *state transition graph* with no outgoing arrows. Ex: stable steady states & cyclic attractors

MaBoSS

Idea of MaBoSS (Markovian Boolean Stochastic Simulator): Fill the gap between ODE and discrete time Boolean formalisms with **continuous time Boolean modeling**



Home Installation How To

1odels Toy Model Cell Cycle Cell Fate p53 / MDM2 Drosophila Patterning

Publication Documentat

he Team

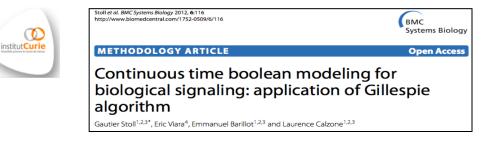
MaBoSS Project

MaBoSS is a C++ software for simulating continuous/discrete time Markov processes, applied on a Boolean network.

Markovian Boolean Stochastic Simulator

MaBoSS uses a specific language for associating transition rates to each node. Given some initial conditions, MaBoSS applies Monte-Carlo kinetic algorithm (or Gillespie algorithm) to the network to produce time trajectories. Time evolution of probabilities are estimated. In addition, global and semi-global characterizations of the whole system are computed.

https://maboss.curie.fr



Application Note

Bioinformatics, in press

MaBoSS 2.0: an environment for stochastic Boolean modeling

Gautier Stoll ^{1,2,3,4*}, Barthélémy Caron ⁵, Eric Viara ⁶, Aurélien Dugourd ⁵, Andrei Zinovyev ⁵, Aurélien Naldi ⁷, Guido Kroemer ^{1,2,3,4,8,9,10}, Emmanuel Barillot ⁵ and Laurence Calzone ^{5,*}

→ Use MaBoSS to quantify the solutions and explore the transient events

Motivation for continuous time algorithm

Synchronized / asynchronized algorithms are defined on discrete time steps.

- → Problems:
- Comparison between model and experimental results mainly on final states (when does a biological experimental system reach its final state?)
- Difficulty of modeling transient effects (e.g. in cell cycle)
- Difficulty of implementing different time scales of events (e.g., a phosphorylation is faster than a transcription)

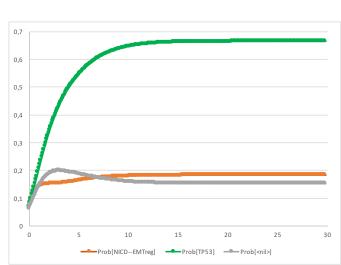
➔ General idea: fill the gap between ODE and discrete time Boolean modeling with continuous time Boolean modeling

The model is defined by:

- Initial condition: probability distribution over network states at time 0
- a rate of change associated to each transition (separate rate up and rate down)

Method: continuous time Markov process / Gillespie algorithm \rightarrow To each Boolean state, a probability is associated over time

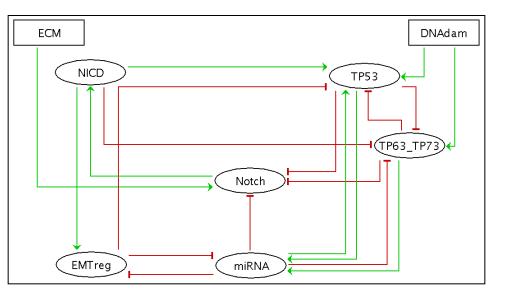
CurrentOp.bnd ~		
Node NICD {	CurrentOp.bnd.cfg ~	
logic = (Notch);	<pre>\$u_NICD = 1;</pre>	
<pre>rate_up = @logic ? \$u_NICD : 0;</pre>	\$d_NICD = 1;	
rate_down = @logic ? 0 : \$d_NICD;	<pre>\$u_Notch = 1;</pre>	
}	<pre>\$d Notch = 1;</pre>	
Node Notch {	\$u TP53 = 1;	
logic = (!miRNA & ECM & !TP53 & !TP63_TP73);	\$d_TP53 = 1;	
<pre>rate_up = @logic ? \$u_Notch : 0;</pre>	\$u TP63 TP73 = 1;	
rate_down = @logic ? 0 : \$d_Notch;		
}	\$d_TP63_TP73 = 1;	
Node TP53 {	<pre>\$u_miRNA = 1;</pre>	
logic = (!NICD & !TP63_TP73 & !miRNA & !EMTreg & DNAdam) (!	\$d_miRNA = 1;	
NICD & !TP63_TP73 & miRNA & !EMTreg) (NICD & !TP63_TP73 & !	\$u_EMTreg = 1;	
EMTreg);	<pre>\$d_EMTreg = 1;</pre>	
rate_up = @logic ? \$u_TP53 : 0;	\$u DNAdam = 1;	
rate_down = @logic ? 0 : \$d_TP53;	\$d_DNAdam = 1;	
1	\$u_ECM = 1;	
Node TP63 TP73 {		
logic = (!NICD & !TP53 & !miRNA & DNAdam);	\$d_ECM = 1;	
rate_up = @logic ? \$u_TP63_TP73 : 0;		
rate_down = @logic ? 0 : \$d_TP63_TP73;	<pre>//[NICD].istate = 1 [0] , 0 [1];</pre>	
}	<pre>//[Notch].istate = 1 [0] , 0 [1];</pre>	
Node miRNA {	<pre>//[TP53].istate = 1 [0] , 0 [1];</pre>	
logic = (!TP53 & TP63_TP73 & !EMTreg) (TP53 & !EMTreg);	<pre>//[TP63_TP73].istate = 1 [0] , 0 [1];</pre>	
<pre>rate_up = @logic ? \$u_miRNA : 0;</pre>	<pre>//[miRNA].istate = 1 [0] , 0 [1];</pre>	
<pre>rate_down = @logic ? 0 : \$d_miRNA;</pre>	<pre>//[EMTreg].istate = 1 [0] , 0 [1];</pre>	
}	<pre>//[DNAdam].istate = 1 [0] , 0 [1];</pre>	
Node EMTreg {		
logic = (NICD & !miRNA);	<pre>//[ECM].istate = 1 [0] , 0 [1];</pre>	
rate_up = @logic ? \$u_EMTreg : 0;		
<pre>rate_down = @logic ? 0 : \$d_EMTreg;</pre>	NICD.is_internal = 0;	
}	Notch.is_internal = 1;	
Node DNAdam {	TP53.is_internal = 0;	
logic = (DNAdam);	$TP63_TP73_is_internal = 0;$	
rate_up = @logic ? \$u_DNAdam : 0;	<pre>miRNA.is_internal = 1;</pre>	
<pre>rate_down = @logic ? 0 : \$d_DNAdam;</pre>	EMTreg.is_internal = 0;	
}		
Node ECM {	DNAdam.is_internal = 1;	
logic = (ECM);	ECM.is_internal = 1;	
rate_up = @logic ? \$u_ECM : 0;		
rate_down = @logic ? 0 : \$d_ECM;	<pre>time_tick = 0.1;</pre>	
}	<pre>max_time = 30;</pre>	
	<pre>sample_count = 50000;</pre>	
	discrete_time = 0;	
	use physrandgen = 1;	
	seed_pseudorandom = 0;	
	display_traj = 0;	
	<pre>statdist traj count = 0;</pre>	
	<pre>statdist_cluster_threshold = 1;</pre>	
	<pre>thread_count = 1;</pre>	
	<pre>statdist similarity cache max size = 20000;</pre>	
	AATAATAATAATAATAATAATAATAATAATAATAA	



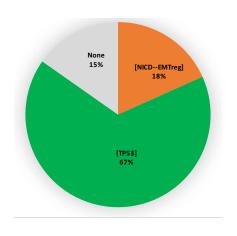
Time trajectories

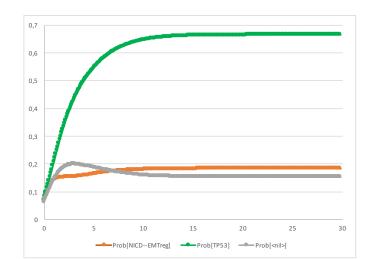


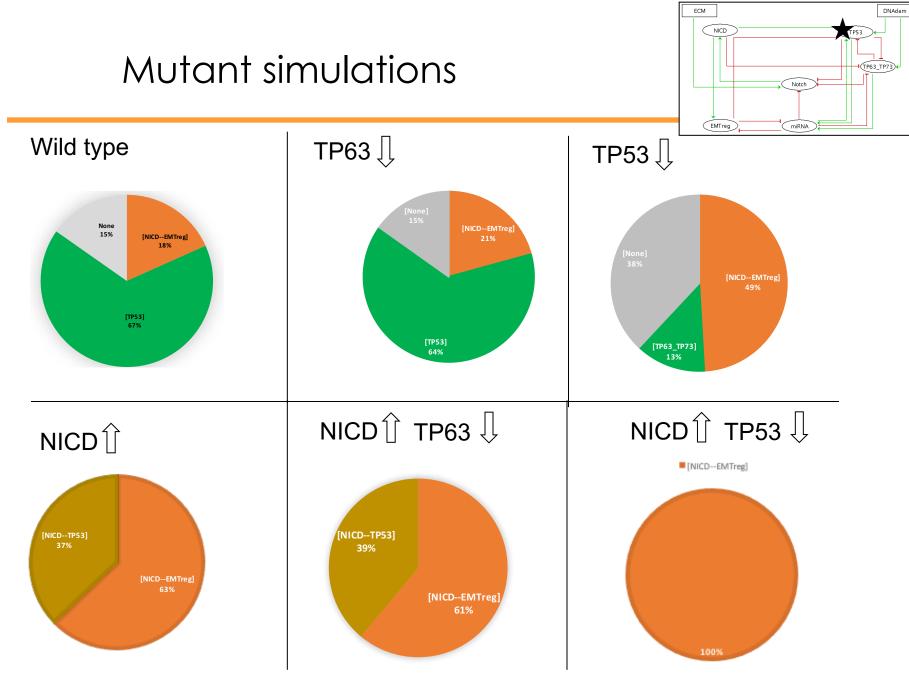
Simulation of the simple network



Probability	DNAdam	ECM	Notch	NICD	miRNA	TP53	TP63_TP73	EMTreg	Phenotypes	
0.12396	0	1	1	1	0	0	0	1	EMT ON	Apoptosis OFF
0.05912	. 1	. 1	1	1	0	0	0	1	EMT ON	Apoptosis OFF
0.12538	0	1	0	0	1	1	0	0	EMT OFF	Apoptosis ON
0.19072	. 1	1	0	0	1	1	0	0	EMT OFF	Apoptosis ON
0.09788	0	0	0	0	1	1	0	0	EMT OFF	Apoptosis ON
0.25044	. 1	. 0	0	0	1	1	0	0	EMT OFF	Apoptosis ON
0.1525	0	0	0	0	0	0	0	0	None	None







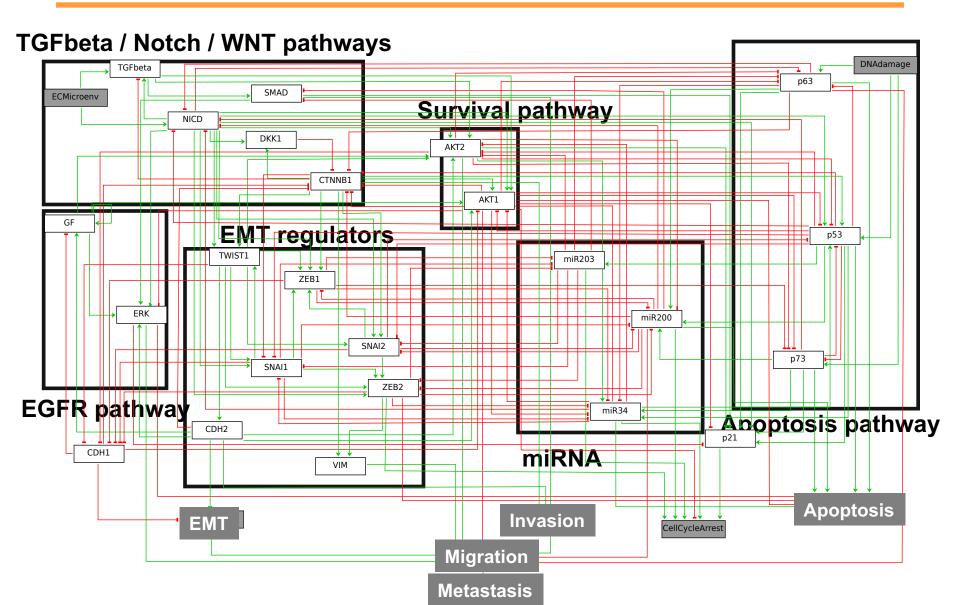
→ coherent with experimental evidence

A more complex view of the process

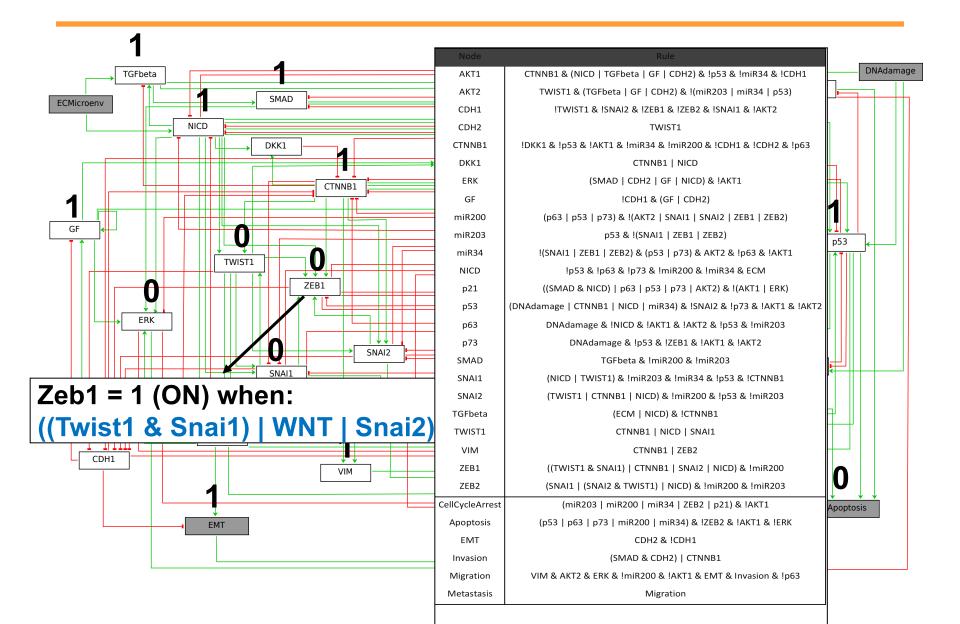
A regulatory network of p53 and Notch pathways

David Cohen

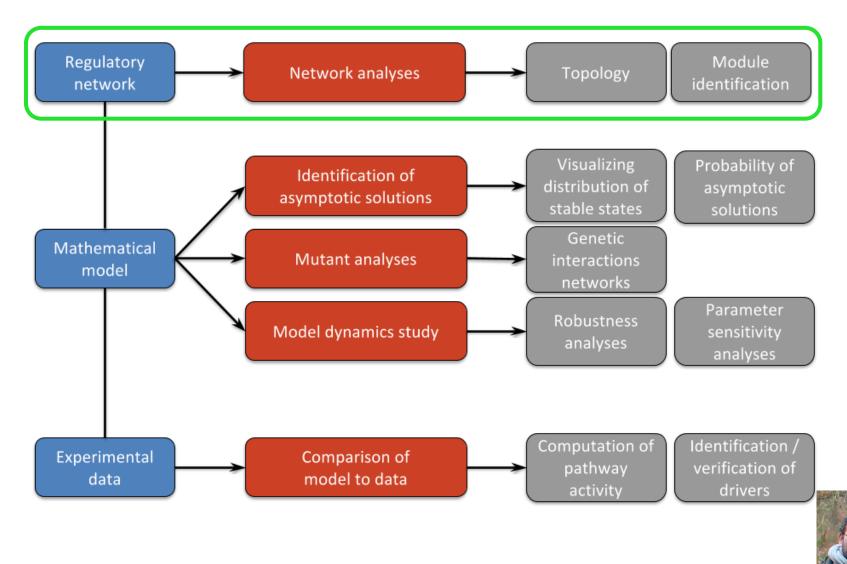
R.



Discrete mathematical model of metastases

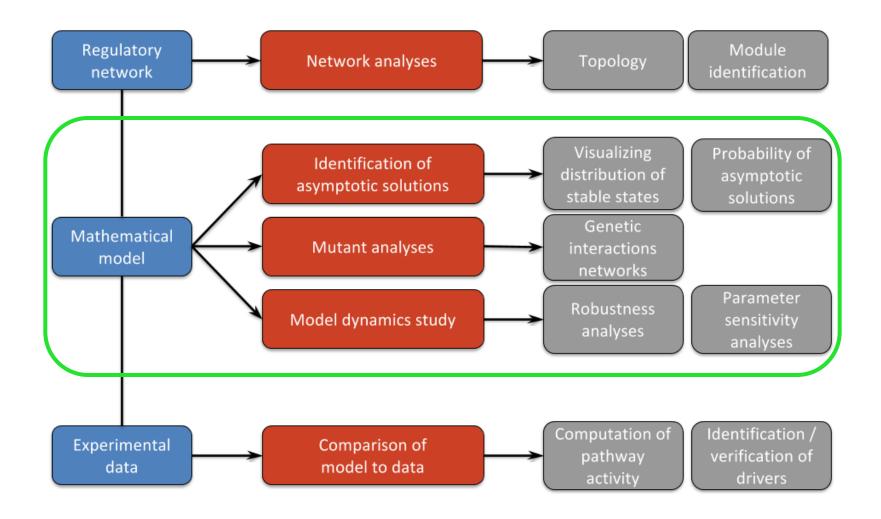


Several analyses can be done on the model

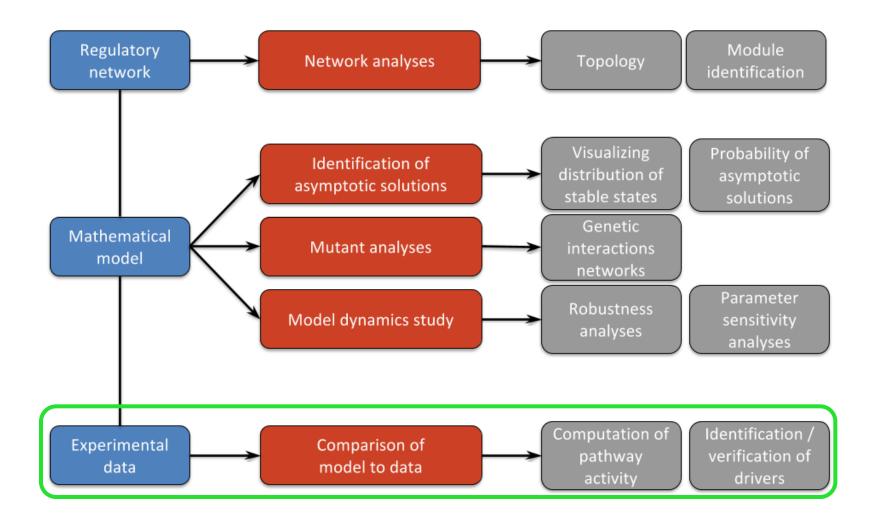


Arnau Montagud

Several analyses can be done on the model



Several analyses can be done on the model

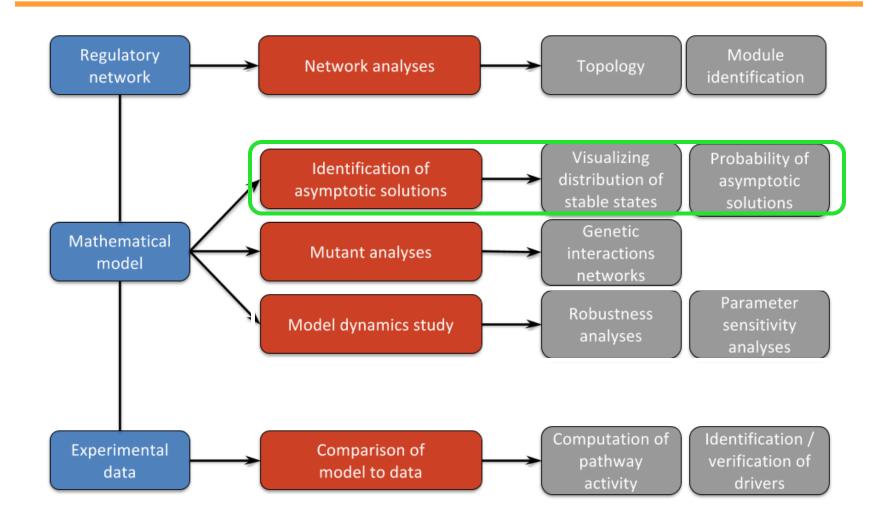


What insights can we get from the mathematical model

Types of questions to be answered

- what are the solutions of the model that can be interpreted biologically?
- what are the important nodes of the network?
- how robust/sensitive is the model?
- can we predict genetic interactions (epistasis, synthetic lethality) from the model?
- what nodes are the most related to a clinical output (e.g. stage of the tumor or metastasis)?

Pipeline



Visualizing distribution of stable states

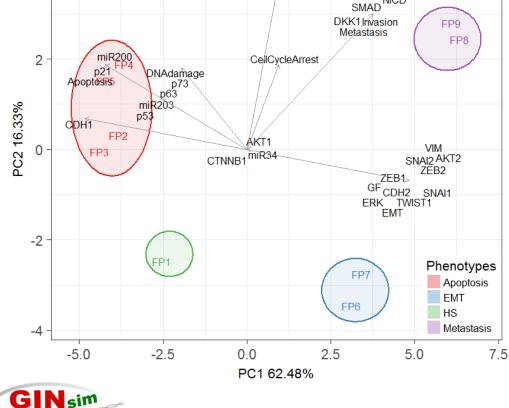
4

	FFI	FFZ	ггэ	ГГ4	ггэ	FFU		FFO	113
	HS	Apop1	Apop2	Арор3	Apop4	EMT1	EMT2	M1	M2
Metastasis	0	0	0	0	0	0	0	1	1
Migration	0	0	0	0	0	0	0	1	1
Invasion	0	0	0	0	0	0	0	1	1
EMT	0	0	0	0	0	1	1	1	1
Apoptosis	0	1	1	1	1	0	0	0	0
CellCycleArrest	0	1	1	1	1	1	1	1	1
ECMicroenv	0	0	0	1	1	0	0	1	1
DNAdamage	0	1	1	1	1	1	0	1	0
GF	0	0	0	0	0	1	1	1	1
TGFbeta	0	0	0	1	1	0	0	1	1
p21	0	1	1	1	1	0	0	0	0
CDH1	1	1	1	1	1	0	0	0	0
CDH2	0	0	0	0	0	1	1	1	1
VIM	0	0	0	0	0	1	1	1	1
TWIST1	0	0	0	0	0	1	1	1	1
SNAI1	0	0	0	0	0	1	1	1	1
SNAI2	0	0	0	0	0	1	1	1	1
ZEB1	0	0	0	0	0	1	1	1	1
ZEB2	0	0	0	0	0	1	1	1	1
AKT1	0	0	0	0	0	0	0	0	0
DKK1	0	0	0	0	0	0	0	1	1
CTNNB1	0	0	0	0	0	0	0	0	0
NICD	0	0	0	0	0	0	0	1	1
p63	0	0	1	0	1	0	0	0	0
p53	0	1	0	1	0	0	0	0	0
p73	0	0	1	0	1	0	0	0	0
miR200	0	1	1	1	1	0	0	0	0
miR203	0	1	0	1	0	0	0	0	0
miR34	0	0	0	0	0	0	0	0	0
AKT2	0	0	0	0	0	1	1	1	1
ERK	0	0	0	0	0	1	1	1	1
SMAD	0	0	0	0	0	0	0	1	1

FP1 FP2 FP3 FP4 FP5 FP6 FP7 FP8 FP9

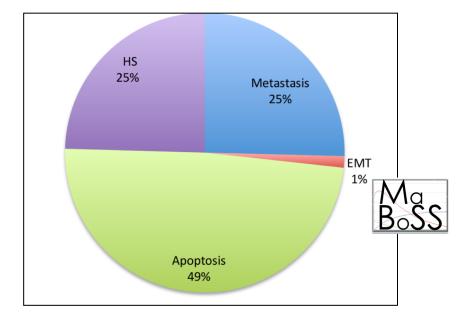
can be classified using PCA **ECMicroenv** TGFbeta FRigration SMAD DKK1 Invasion Metastasis miR20 CellCvcleArrest p21 DNAdamage p63 Aboptosis miR203 p53 **CDH1**

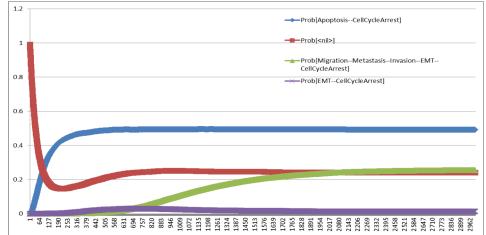
The solutions of the model



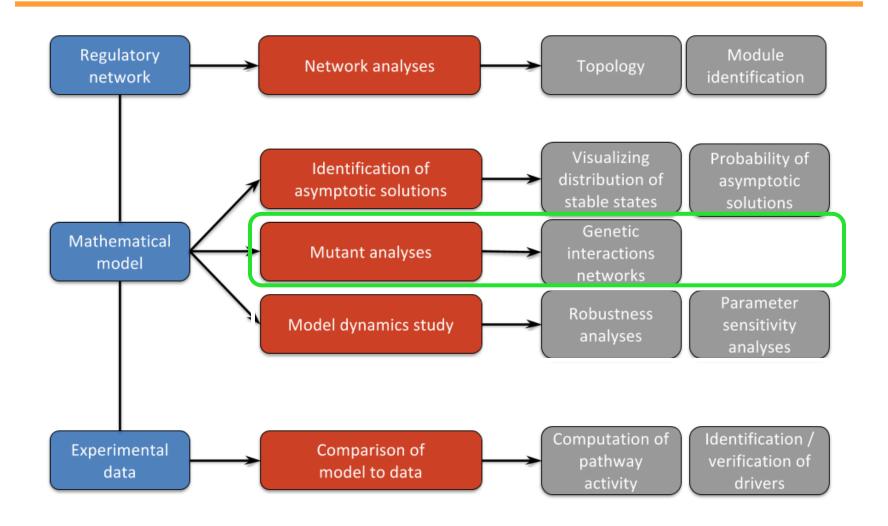
Probability of asymptotic solutions

FP1 FP2 FP3 FP5 FP6 FP7 FP8 FP9 FP4 HS Apop1 Apop2 Apop3 Apop4 EMT1 EMT2 M1 M2 Metastasis Migration Invasion EMT Apoptosis CellCycleArrest ECMicroenv DNAdamage GF TGFbeta p21 CDH1 CDH2 VIM TWIST1 SNAI1 SNAI2 ZEB1 ZEB2 AKT1 DKK1 CTNNB1 NICD p63 p53 p73 miR200 miR203 miR34 AKT2 ERK SMAD



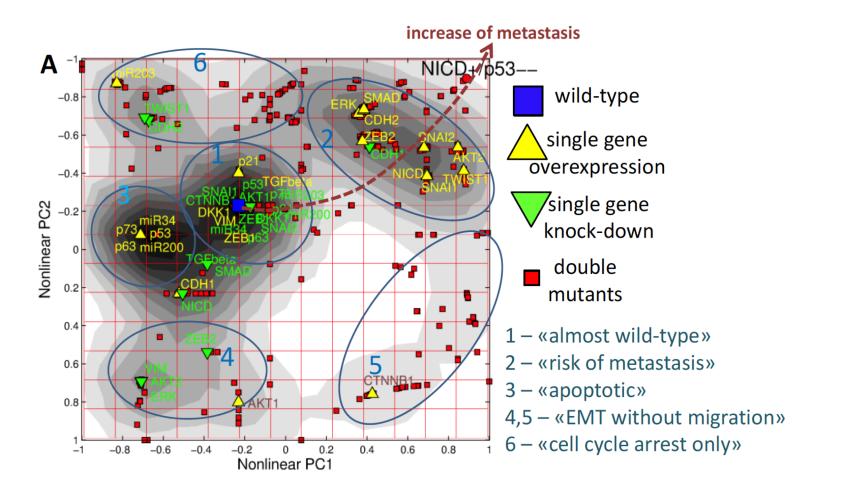


Pipeline

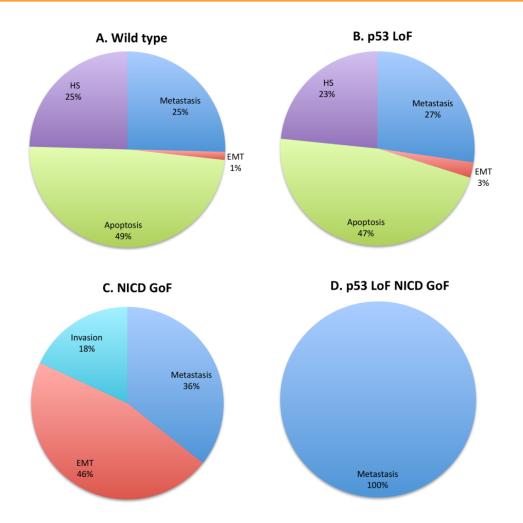


Map of *in silico* single and double mutations

- Automatic simulation of single and double mutants
- Quantification of probabilities to reach metastasis for all single and double mutants



What about the double mutant accounting for alterations in the Notch and p53 pathways



The model confirms the metastatic phenotype in the Notch++/p53-- double mutant

Predicting **genetic interactions** from the genes of the model with respect to metastasis

4 genetic interactions drastically increase metastasis:

NICD GoF - p53 LoF NICD GoF - p73 GoF

NICD GoF - SNAI2 GoF NICD GoF - AKT2 GoF

⇒ amplifier mechanisms for appearance of metastasis in NICD GoF mutants

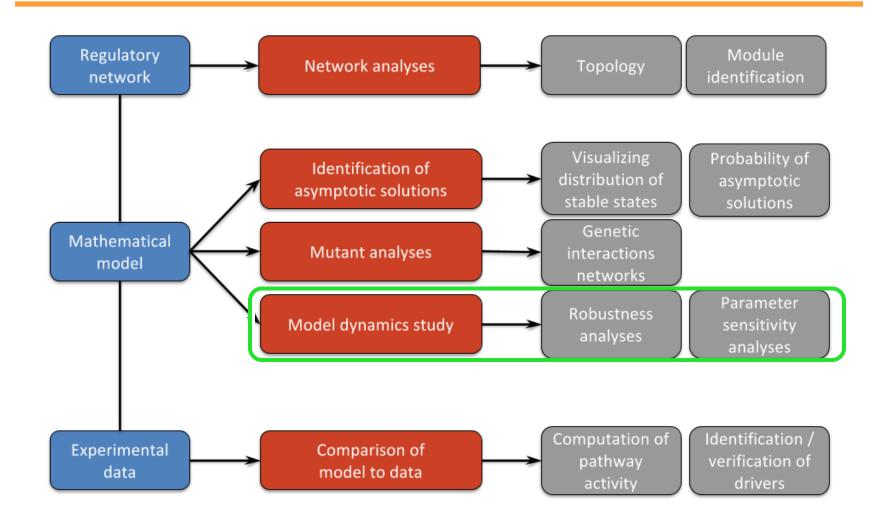
₁CDH2AK Β WIST1 CTNNB GFß miR200 SMAD **ERK** miR203 miR34 TWIST/1 SNAI2 SNA AKT2 NICD **Γ**GFβ SMAN single gene overexpression ′p53 single gene synergistic interactions knock-down masking interactions

> nodes: single mutants edges: type of epistatic interactions thickness of edge: epistasis value

Calzone L, Barillot E, Zinovyev A. Predicting genetic interactions from Boolean models of biological networks. Integr Biol. 2015;7(8):921-9.

Cohen DP, Martignetti L, Robine S, Barillot E, Zinovyev A, Calzone L. Mathematical Modelling of Molecular Pathways Enabling Tumour Cell Invasion and Migration. PLoS Comput Biol. 2015 Nov 3;11(11):e1004571.

Pipeline



Robustness analyses

- Robustness of a phenotype to mutations
 ex: Does a mutant enhance or diminish the probability to reach the
 Metastasis node? Which mutant alters the most the phenotype?
- 2. Robustness of logical gates with respect to a phenotype Is the model unique?
- 3. Robustness of logical gates with respect to stable states How does a change in the model affect the stable states?

Robustness of the logical gates with respect to the phenotype probability

- Can we confirm that the proposed model is robust with respect to small changes of logical rules?
- Is there one model or a family of models that could be equivalent?
- Can we identify the "weak spots" of the model?

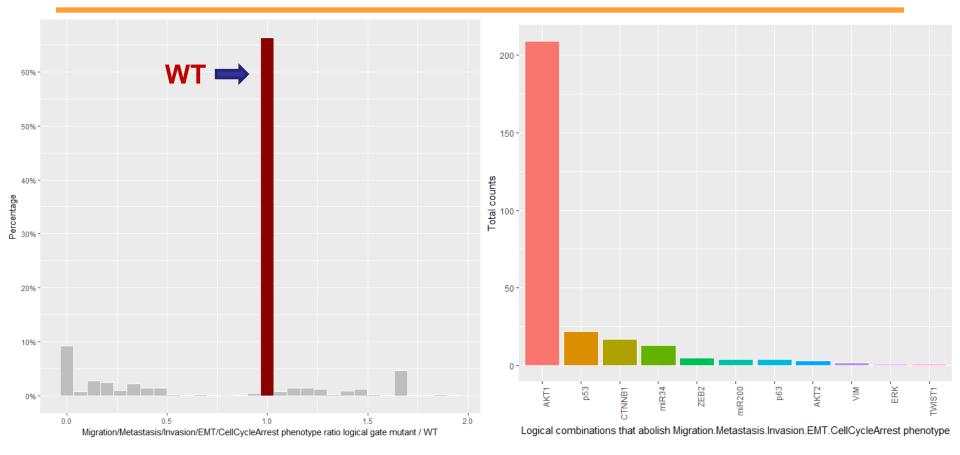
Three tests were performed on logical rules

- One operator in all rules was changed
 - Two operators in one rule were changed
- One operator in two rules was changed

(from AND to OR and vice versa)

Question: how do these changes affect the probability to reach a phenotype?

Robustness of the logical gates with respect to the phenotype probability



- The model is quite robust with respect to all phenotypes
 - Metastasis is the least robust
- The rules of some genes need to be more stringent: AKT1 and p53 in particular (anti-migratory)

https://github.com/sysbio-curie/Logical_modelling_pipeline

🛛 sysbio-curie / Logical_model	O Watch 1 ★ Star 1 % Fork 1				
<> Code ① Issues 0 ① Pull re	equests 0 🗐 Projects 0 🗐 Wiki 🔟 Insights				
Branch: master - Logical_modelling	g_pipeline / scripts /	Create new file Find file History			
ArnauMontagud corrected Analyses I	Latest commit 55ccf0c 8 days ago				
1 run MaBoSS	BND_CFG file changed	12 days ago			
2 PCA on ss	modified stewd in R scripts and new md file in doc folder	28 days ago			
3 Displaying asymptotic solutions	modified stewd in R scripts and new md file in doc folder	28 days ago			
4 Predicting genetic interactions	updating correct ginsimout	29 days ago			
5 Analyses of genetic interactions	modified stewd in R scripts and new md file in doc folder	28 days ago			
6 Predicting logical gates interac	updating correct ginsimout	29 days ago			
7 Analyses of logical gates	corrected Analyses of logical gates	8 days ago			
8a Using the model as a scaffold	Updating ROMA files	28 days ago			
8b Using data as priors of model	Updating ROMA files	28 days ago			
8c Using data as priors of model	adding stewardship script to run sections 1 through 7 at on	ce, minor a month ago			
🖿 run all analyses	corrected Analyses logical gates	8 days ago			



Contributors

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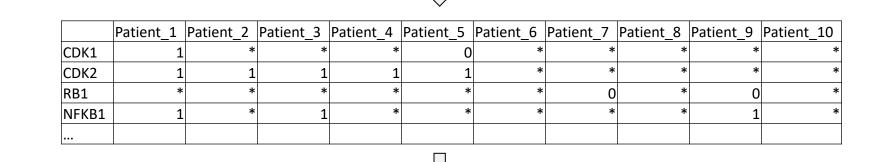
Improvements of the pipeline

- Automatic search for node inhibition: suggestion of drug targets (already possible with MaBoSS)
- Automatisation of several tasks: choose what to do and launch several tasks in one simulation (already possible but needs optimisation)
- Contextualisation of models to patient data in progress
- Integration of logical models into agent-based models in progress

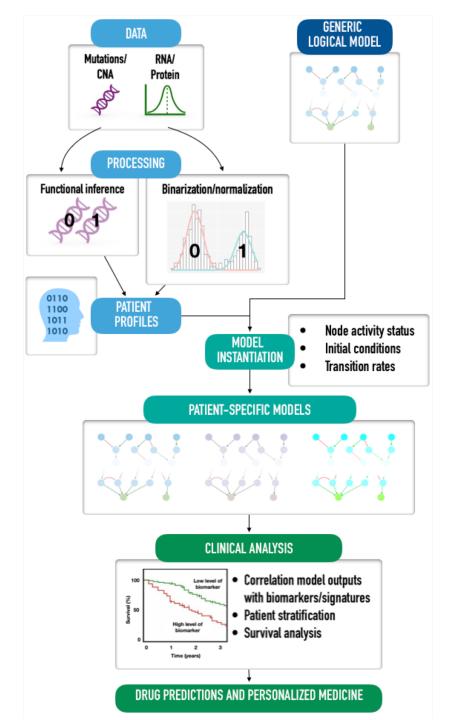
Contextualisation of models to patient data

⇒ Compute the probability of a phenotype per patient (or groups of patients) → specify a model to a patient

	Patient_1	Patient_2	Patient_3	Patient_4	Patient_5	Patient_6	Patient_7	Patient_8	Patient_9	Patient_10
CDK1	0.34980	-3.63820	-1.64350	-1.12862	-1.48949	-1.14924	-3.13846	-3.97786	-0.77106	-1.08848
CDK2	0.79515	-1.45574	0.21421	-1.22189	-0.28390	-2.77291	-1.71527	-2.04611	0.27713	-0.21242
RB1	1.51308	-1.01982	-0.28808	-0.10028	-0.25528	-0.51715	-0.32806	-0.95599	0.26762	0.02276
NFKB1	0.32836	0.47176	0.45348	0.02632	-0.88051	-0.13897	-1.78039	-0.86474	0.46306	-0.08317



Patient 1: Probability of proliferation increased when compared to normal condition?



1. Start with a model and some patient data

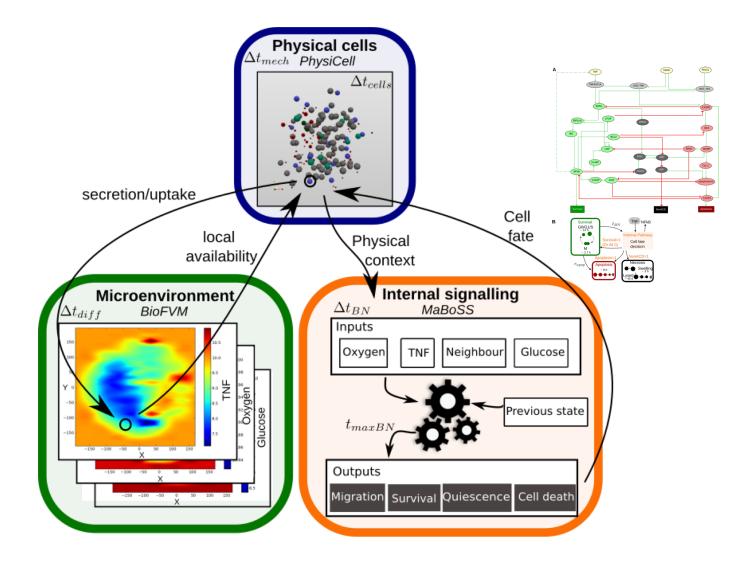
2. Binarize or normalize the data

- 3. Build individual patient profiles mutations + CNV = mutants expression data = speed of reactions
- 4. Simulate each patient

5. Correlate results to clinical data (survival curves, proliferation index, size of the tumour, etc.)

Béal et al., Submitted

Integration of logical models into agentbased models

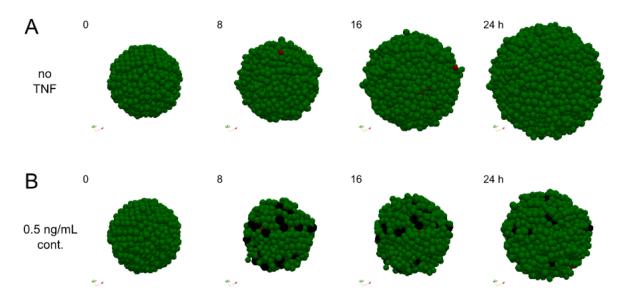


Integration of a logical (MaBoSS) model into an agent-based tool: PhysiBoSS

Example of model of cell fate decision:

A) in proliferating conditions (cells divide every 16 hours)

B) treated with TNF (Tumor Necrosis Factor) in proliferating conditions



Green: proliferating cells Red: apoptotic cells Black: necrotic cells

→ In silico experiment shows that tumour does not grow as fast when treated with TNF
 → Possibility to test effect of treatment on heterogeneous cell population (clonality)
 → Possibility to test different types of treatments (pulses or continuous)

Acknowledgements The modelling team



Thank you for your attention