Drop Shaping by Laser-Pulse Impact

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We show how the deposition of laser energy induces propulsion and strong deformation of an absorbing liquid body. Combining high speed with stroboscopic imaging, we observe that a millimeter-sized dyed water drop hit by a millijoule nanosecond laser pulse propels forward at several meters per second and deforms until it eventually fragments. The drop motion results from the recoil momentum imparted at the drop surface by water vaporization. We measure the propulsion speed and the time-deformation law of the drop, complemented by boundary-integral simulations. The drop propulsion and shaping are explained in terms of the laser-pulse energy, the drop size, and the liquid properties. These findings are, for instance, crucial for the generation of extreme ultraviolet light in nanolithography machines.

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I. INTRODUCTION

A laser-induced phase change in liquids can lead to a violent response: deformation and disruption of the liquid body followed by the ejection of matter. The complete vaporization or even explosion of micrometer-sized drops can result from the linear absorption of laser energy [1–3]. Self-focusing and dielectric breakdown may lead to plasma formation in transparent drops [4–7]. Laser impact has been used to generate liquid motion by vaporization or plasma formation in confined geometries [8–10], sessile drops [11], and biological matter [12–14].

Here, we show how the absorption of laser energy by an unconfined liquid drop induces a rapid phase change (see Fig. 1), which in turn controls the propulsion, expansion, and fragmentation of the drop. A key application of the drop shaping by laser impact is found in laser-produced plasma light sources for extreme ultraviolet (EUV) nanolithography [15,16]. In these sources the shape, position, and stability of a liquid-tin body directly affect the conversion efficiency of liquid tin to a plasma that emits EUV light.

The detailed understanding of the hydrodynamic response of an opaque liquid drop to laser impact poses two fundamental challenges. First, one needs to resolve how momentum is transferred from the laser to the drop. Second, the subsequent deformation dynamics and fragmentation of the drop after impact have to be quantified. Although drop impact onto a solid substrate has been studied thoroughly (for a selection, see, e.g., Refs. [18–24]), no consensus on the deformation dynamics has yet been reached and only few studies [19,20, 25–27] focused on the fragmentation.

II. EXPERIMENTAL METHODS

Our model system consists of a highly absorbing drop that is hit by a pulsed laser beam. In Fig. 2 an overview of the experimental setup is shown. The drop detaches from a capillary, falls, and relaxes to a spherical shape with radius...
is determined in separate measurements, for which the top beam dump shown in Fig. 2 is replaced by an energy meter. A focusing lens decreases the beam diameter to twice the drop size in order to achieve a uniform but high-intensity illumination of the drop. To ensure the drop is placed at the center of the laser beam, the drop position is optimized such that the drop-shape evolution is axisymmetric with respect to \( \tilde{e}_z \) and the propulsion speed is maximum.

The energy \( E \) that is actually absorbed by the drop is computed from a beam-profile measurement and ray tracing [28]. The typical beam fluence 1 J/cm² is well below the dielectric breakdown and self-focusing thresholds reported for water with focused nanosecond laser pulses [8,17]. Consistently, we observe a plasma only when the laser beam is tightly focused inside the drop [Fig. 1(a), see also Refs. [12,13]], but not for a uniform irradiation [Fig. 1(b)]. To visualize the wavelengths in the visible spectrum that are emitted by the drop shown in Fig. 1, we use a magenta-colored ink as a dye and a color camera. For all experiments leading to quantitative results we use a black-colored ink to suppress fluorescence.

The postimpact dynamics of the drop [Fig. 3(a)] is observed from a side view (\( \tilde{e}_z \) axis in Fig. 2) with a long-distance microscope, a high-speed camera operated at a frame rate of 20 000 frames/s, and a continuous light source. Detailed information in the first microseconds after impact is obtained by operating a camera in stroboscopic mode with a flash lamp that delivers a high-intensity light pulse of 8 ns [Fig. 3(b)]. We record stroboscopic videos by performing a single-impact experiment per video frame while changing the time delay between the laser impact and the pulsed light source. For both cameras used, the size of the field of view is \( 16 \times 10 \text{ mm}^2 \), which yields a pixel resolution of 16 \( \mu \text{m} \) per pixel.

### III. Results and Interpretation

The drop dynamics for different pulse energies is shown in Fig. 3. On impact, the surface of the drop hit by the laser emits a shock wave into the air [Fig. 3(b)]. The shock wave is followed by the ejection of a mist cloud of small drops that is visible as a gray-to-black haze in the images and persists for several microseconds. Subsequently, the mist is expelled while the drop propels in the opposite direction [Fig. 3(a)]. At the same time the drop flattens and expands in the radial direction before it either retracts, for low pulse energy, or fragments, for large energy.

We quantify the drop motion by measuring the displacement \( Z(t) \) of the drop center of mass and the drop radius \( R(t) \) [defined in Fig. 3(a)] for the first milliseconds after impact. As Fig. 4(a) shows, the drop is propelled at a constant speed \( U \) that increases with increasing pulse energy up to 2.0 m/s. The accompanying deformation of the drop occurs on the inertial time scale \( \tau_i = R_0 / U \sim 10^{-4} \) to \( 10^{-3} \) s [Fig. 4(b)] and is eventually slowed down by...
surface tension on the capillary time scale $\tau_c = \sqrt{\rho R_0^3/\gamma} = 3.5$ ms. Both the initial deformation rate $\Gamma_i^{-1}$ and the maximal extension $R_{\text{max}}$ increase with increasing pulse energy. We emphasize the clear separation of time scales

$$\tau_p \ll \tau_c \ll \Gamma_i < \tau_c$$

between the successive steps, namely, the laser pulse, the ejection of matter (on the time scale $\tau_e \sim 10^{-5}$ s), the initial deformation of the drop, and its capillary retraction.

To explain the relation between the drop-propulsion speed, the radial expansion, and the laser energy one needs to understand the mechanism that propels the drop. Surely, both the optical-radiation pressure from the laser and the thermal-radiation pressure caused by the heating of the drop surface are insignificant [29,30]. The motion actually results from the recoil due to the partial vaporization of the drop: since the highly absorbent dye ensures that the laser energy is absorbed in a superficial layer on one side of the drop, the vapor expulsion is mainly unidirectional and consequently transfers momentum to the remainder of the drop.

The light energy is absorbed by a liquid mass $\sim \rho R_0^2 \delta$ set by the penetration depth of the laser. On the time scale $\tau_e$, both diffusive and radiative heat transfers are negligible (the thermal diffusion length is much smaller than $\delta$ [31]). Since the beam profile is flat, and neither the focusing due to the drop-interface curvature nor nonlinear optical effects (self-focusing or electric breakdown) are significant, we consider the energy deposition in the superficial layer to be close to uniform. This energy is sufficient to heat the liquid from the ambient temperature $T_0 = 293$ K to the boiling temperature $T_b = 393$ K, but not to vaporize all of it. Only a certain fraction $\beta$ actually vaporizes. The energy balance therefore reads $E \sim \rho R_0^2 \delta c_v (T_b - T_0) + \beta \Delta H$, where $c_v = 4.0$ kJ/(kg K) and $\Delta H = 2.25$ MJ/kg are, respectively, the specific heat capacity and latent heat of vaporization of the liquid.

In all of our experiments a mist cloud is observed, which is a clear signal of a local boiling of the drop. We therefore assume that to get propulsion, a threshold energy $E_{\text{th}} \sim \rho R_0^2 \delta c_v (T_b - T_0) \approx 3$ mJ has to be absorbed by the superficial layer to heat the liquid to the boiling point, which is in good agreement with the threshold for propulsion observed in our experiments [Fig. 5(a)]. Any additional energy deposited in the superficial layer is used to vaporize a mass of liquid $m \sim \beta \rho R_0^2 \delta (E - E_{\text{th}})/\Delta H$. An upper limit for the proposed scaling is given by $E/E_{\text{th}} \sim 1 + \Delta H/[c_v(T_b - T_0)] \approx 8$, in which case the absorbed energy is sufficient to evaporate the entire heated liquid layer (i.e., $\beta = 1$). Any increase in $E$ beyond this point would
lead to a superheated or even a critical phase, in which case the opaque mist cloud would not be observed \[13\].

For \(0 < \beta < 1\), which is the case of our experiments, the remaining part of the heated layer that is not vaporized is expelled as a mist of small drops. We assume that the liquid vaporizes at \(T_h\) and that the vapor is expelled at the thermal speed \(u = \sqrt{k_B T_h / \mu} \approx 400\) m/s, where \(k_B = 1.38 \times 10^{-23}\) J/K is the Boltzmann constant, and \(\mu = 2.99 \times 10^{-26}\) kg is the molecular mass of water. This expelled vapor propels the remainder of the drop. Momentum conservation \(mu = \rho R_0^3 U\) yields

\[
U \sim \frac{E - E_{th}}{\rho R_0^3 \Delta H} u, \tag{2}
\]

that is, an increase in \(U\) proportional to that in \(E\). Figure 5(a) shows that this scaling argument, with a prefactor of 0.4, is in good agreement with our experimental data.

With a description of the propulsion at hand, we now turn to the drop deformation. The expansion dynamics is directly affected by surface tension, which promotes the retraction and possibly the fragmentation of the drop. The key parameter describing the expansion is therefore the Weber number of the motion induced by the laser \(\text{We} = \rho R_0 U^2 / \gamma\), which compares the drop-displacement kinetic energy to its surface energy. In our experiments \(1 \leq \text{We} \leq 60\). The impulsive acceleration of our drop from 0 to \(U\) is similar to the impulsive stop of a drop impacting a solid with velocity \(U\). We therefore use the momentum-based scaling derived by \[18,20\] for drop impact on solids to express the maximal radial expansion

\[
\frac{R_{\max} - R_0}{R_0} \sim \text{We}^{1/2} \sim \sqrt{\frac{\rho R_0 u^2 E - E_{th}}{\gamma \rho R_0^3 \Delta H}}, \tag{3}
\]

in which the expression in terms of \(E\) directly comes from Eq. (2). Expression (3), with a prefactor of 0.6, is in good agreement with our experimental data up to \(\text{We} \sim 40\), when the drop starts fragmenting and the maximum expansion saturates [see Fig. 5(b)]. The scaling (3) has already been observed for drop impact onto solid substrates with negligible friction [20]. The present setup is, however, fundamentally different since, as mentioned above, the typical impact time scale, during which the drop accelerates, is decoupled from the inertial time scale: \(\tau_c \ll \tau_i\).

\section*{IV. NUMERICAL RESULTS}

To confirm that the interaction of the laser pulse with the drop can be modeled as a short recoil-pressure pulse exerted on the drop surface, we perform boundary-integral (BI) simulations \[32–34\]. We assume that the flow inside the drop is inviscid, irrotational, and incompressible, and solve the resulting Laplace equation for the flow potential. The method assumes axisymmetry and therefore cannot be used to study the eventual fragmentation of the drop, but it does capture the initial phase of the drop deformation.

The laser pulse is modeled by applying a pressure boundary condition at the drop surface for a time duration of the fragmentation.
In the present case the laser energy is absorbed in a superficial layer of the drop such that the deposited energy per unit mass \( E/\rho R_0^2 \delta \sim 0.1 \) to 1 MJ/kg is comparable to the specific latent heat of vaporization. As a consequence, drop motion is induced by the recoil due to vaporization on the face of the drop that is hit by the laser. This results in a propulsion speed and a maximal radius of expansion that are both proportional to the pulse energy. The expansion dynamics is limited by surface tension and is similar to that of a drop impacting a solid, although with a laser-pulse momentum transfer takes place on a much shorter time scale. Laser-induced drop fragmentation and the influence of the beam focusing require detailed studies and are left for future work [35]. All results reported here should transpose directly to the shaping of liquid-tin drops in EUV light sources. In a regime where a plasma is generated the propulsion mechanism may change, however, the Weber number remains the key parameter governing the hydrodynamic response.

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V. CONCLUSIONS

We show that an opaque free-falling drop hit by a laser pulse propels and expands until fragmentation occurs.

\[ \tau_e \ll \tau_i. \]

We use a Gaussian pressure profile with a length scale based on the measured laser-beam profile and a pressure scale set to match the propulsion velocity observed in the experiment. This pressure scale is prescribed by the momentum conservation \( pR_0^2 \tau_e \sim pR_0^3U \) (the prefactor can be obtained analytically [35]). From Eq. (2) this recoil pressure can readily be expressed in terms of the absorbed energy.

The numerical drop-shape evolution is shown in Fig. 6. It illustrates the added value of the simulations: not only the two-dimensional projection of the drop shape, but also the spatial and temporal evolution of the sheet thickness can be extracted, which is crucial when it comes to the study of fragmentation [20]. Moreover, Fig. 6 shows that the BI model quantitatively predicts the radial drop expansion observed for different Weber numbers. This confirms that a pressure pulse applied at the drop surface for a time much shorter than the hydrodynamic time scales (\( \tau_i \) and \( \tau_e \)) is indeed sufficient to describe the hydrodynamic response of a drop to the impact of a laser pulse.


29. The typical impulse I exerted on the drop by the 3% reflected light from the surface scales as I ∼ Er/ε, with Eε the energy of the reflected light and ε the speed of light. This impulse would yield a typical drop speed U ∼ 10^-3 m/s. The impulse due to thermal radiation from the hot drop surface scales as I ∼ cεσT^4R^2/R_0^2/c with c the Stefan-Boltzmann constant. This impulse would yield U ∼ 10^-15 m/s.


31. On the time scale of vapor ejection τ_v, heat typically diffuses over a length δ = κτ_v/κ ∼ 10^-6 m ≪ δ, where κ is the thermal diffusivity of water.


Here, we first describe how the energy absorption in the drop is measured. Second, we explain the apparent acceleration of the drop that is visible in Fig. 4 of the main paper “Drop shaping by laser-pulse impact”.

MEASUREMENT OF ENERGY ABSORPTION

We first measure the laser beam profile at the drop location (Fig. 1). To avoid saturation of the beam profiler we attenuate the laser energy by a factor of $10^6$ with two wedged windows and a reflective neutral-density filter. To determine the fraction of the light that is refracted into the drop at the air-liquid interface we use ray tracing (valid for $R_0 = 532$ nm). Since the dye is highly absorbent ($\delta \ll R_0$), we neglect any light transmission through the drop. The initial condition of the ray tracing is set by the focal length of the focusing lens and the position of the drop in the laser beam (see Fig. 2 in the main paper). The distribution of rays in space and the energy attributed to each ray is chosen such that the set of rays resembles the measured beam profile. As a result, we estimate that in our experiments 20% of the laser-pulse energy is absorbed by the drop.

FIG. 1. (Color online) Normalized fluence of the laser beam measured at the drop location by a CCD beam profiler (BC106-VIS by Thorlabs). The profile depicted is the mean result of 10 single measurements. The dotted line indicates the position of the drop during the laser-impact experiments.

FIG. 2. (Color online) Center-of-mass displacement $Z$ of the drop (along $\tilde{e}_z$, see Fig. 2 of the main paper) as a function of time in the BI simulation for $E = 24$ mJ. The blue dashed line represents the actual centre-of-mass displacement, whereas the red solid line is the centre-of-mass displacement based on the two-dimensional projection of the simulated drop shape, which shows an artificial deceleration.

MEASUREMENT OF DROP DISPLACEMENT

For each recorded image we determine the center-of-mass position assuming rotational symmetry of the two-dimensional drop shape. Thereby, we ignore the concavity of the drop shape, which introduces an error in the determination of the centre-of-mass position. This causes an apparent acceleration on the time-scale $\tau_c$ in $Z$ (visible in Fig. 4 of the main paper).

To confirm that this acceleration is an artificial result of our algorithm, we use the results from the BI simulations. In BI the full three-dimensional axi-symmetric shape of the drop is known, and hence the exact centre-of-mass displacement can be determined (dashed, blue line in Fig. 2). In addition, we compute the centre-of-mass displacement based on the two-dimensional projection of the BI data using the same procedure as we apply to the experimental side-view images (solid, red line in Fig. 2). The centre-of-mass determined from the two-dimensional projection shows an artificial deceleration as soon as the drop shape becomes concave. However, Fig. 2 also shows that the final speed of the deforming drop is not affected by the apparent initial deceleration. Therefore, the error introduced by considering the projected drop shape only affects the initial deceleration of the centre-of-mass, not its final speed.